$\qquad$ Pre-Calculus

## I. Analyze the Graph of a Rational Function

1. Factor numerator \& denominator.
2. Write $R$ in lowest terms. Find domain.
3. Locate intercepts.
4. Locate vertical asymptotes.
5. Locate horizontal or oblique asymptotes. Determine if $R$ intersects this asymptote.
6. Use a graphing calculator to help graph R by hand.


## II. Examples

1. $R(x)=\frac{2 x^{2}-5 x+2}{x^{2}-4}$

2. $R(x)=\frac{2 x^{2}-5 x+2}{x^{2}-4}$

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3. $R(x)=\frac{x^{4}+1}{x^{2}}$
4. $R(x)=\frac{3 x^{2}-3 x}{x^{2}+x-12}$

